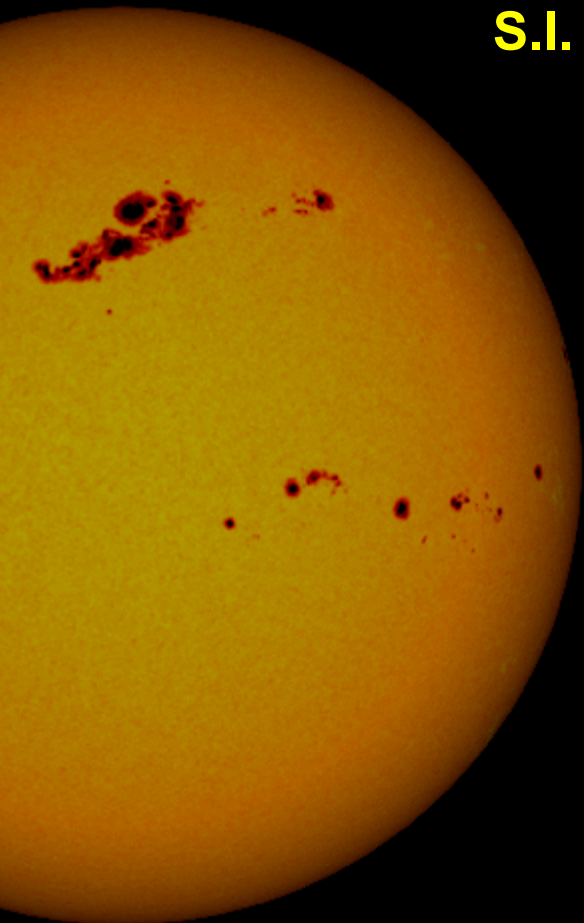


# ACTIVE CAVITY RADIOMETER IRRADIANCE MONITORS 1,2 & 3 S.I. MEASUREMENT UNCERTAINTIES



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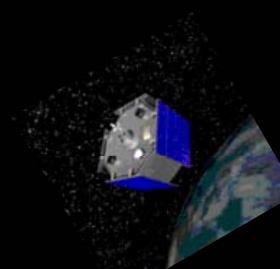
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SMM/ACRIM1

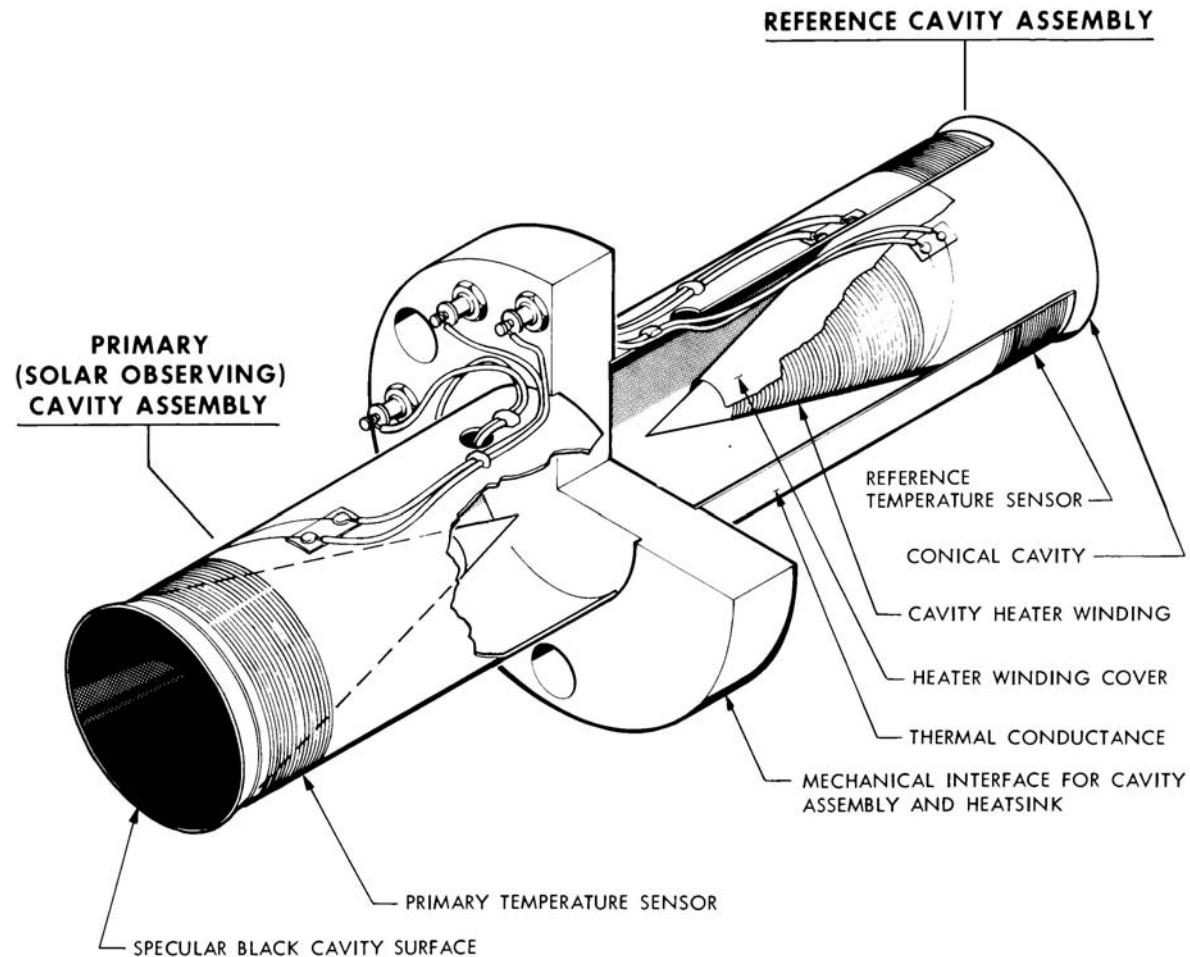


UARS/ACRIM2

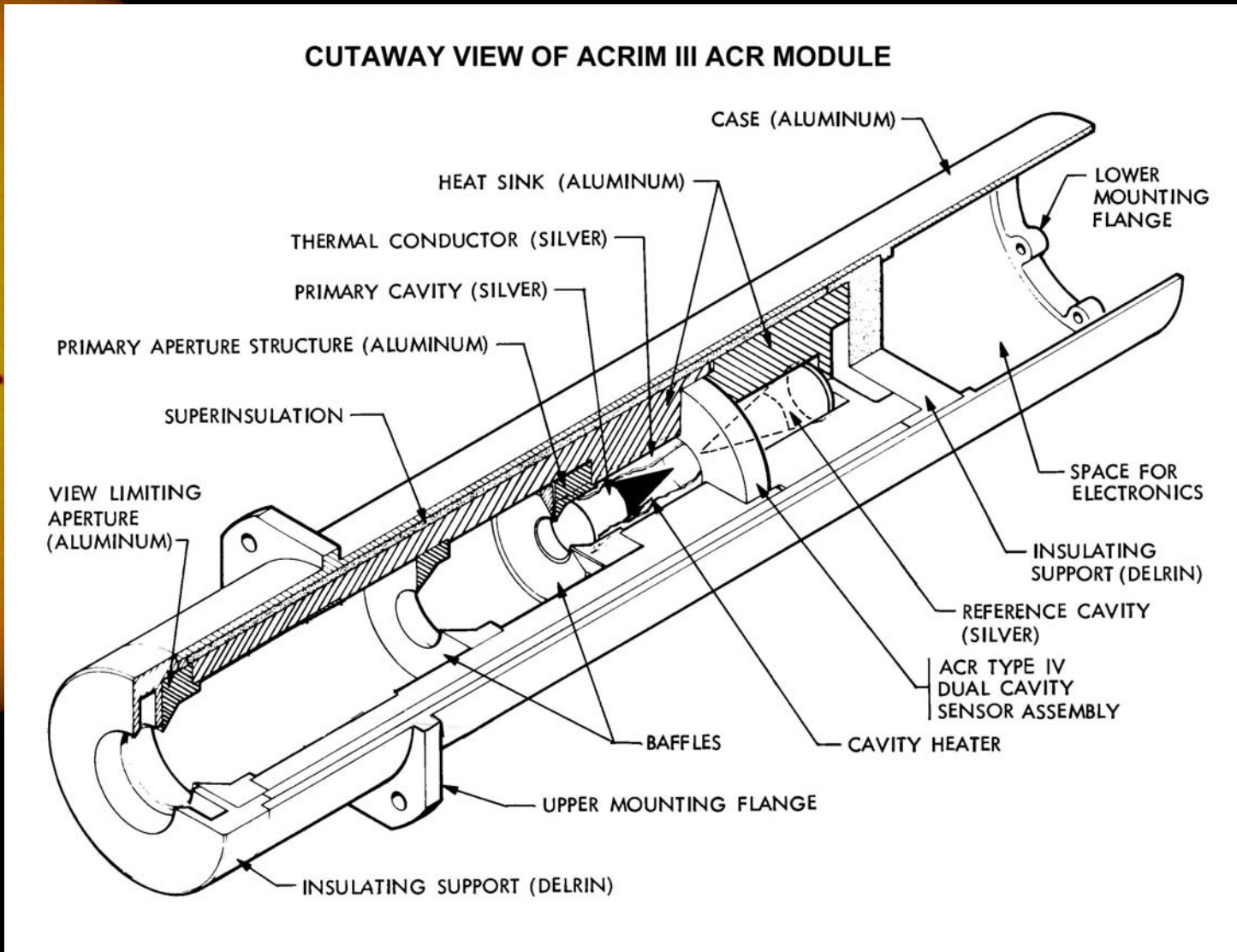


ACRIMSAT/ACRIM3

# Active Cavity Radiometer Type 4



# Active Cavity Radiometer Sensor Module



# Active Cavity Radiometer measurements

- Discussion of the Active Cavity Radiometer design

The ACR employs differential operation

Irradiance measurements depend only differences in the thermal state of the cavity and its surround between reference and observation phases of measurement

ACR design concept is to maximize thermodynamic equivalence of the cavity in reference and observation phases by minimizing the effects of the many small temperature dependent terms.

ACR design concept is to minimize thermal drifting without active controls.

Studies of temperature drift effects, using characteristic values of the radiometer parameters and heat transfer modeling based on the above relationships, indicate temperature difference errors under most conditions are below the threshold of error defined by basic radiometer metrology.

# Active Cavity Radiometer measurements

- Basic properties of the Active Cavity Radiometer (ACR)

Eq. 1  $H = K (P_{er} - P_{eo}) + E$

Where:

$H$  = measured irradiance

$K$  = standard detector constant of proportionality

$P_{er}$  = cavity electrical heater power in the reference mode

$P_{eo}$  = cavity electrical heater power in the observation mode

$E$  = error terms (departures from quasi-equilibrium assumptions)

Axial rays undergo six reflections in the ACR cavity's specular, 30 deg. right circular cone the effective cavity absorptance is:

Eq. 2.  $\alpha_c = 1 - \rho_c^6$

Where:

$\alpha_c$  = effective cavity absorptance

$\rho_c$  = absorptance of cavity surface

6 = number of reflections per axial ray



# Active Cavity Radiometer measurements

- Derivation of the ACR quasi-equilibrium equation

In the reference phase (shutter closed) the input and output power to the cavity are:

Eq. 3. 
$$P_{inr} = P_{er} + \sum_j P_{rcr_j} + P_{hcr}$$

Eq. 4. 
$$P_{outr} = P_{cr} + \sum_j P_{crr_j} + P_{lcr}$$

In the observation phase (shutter open) the input and output power to the cavity are:

Eq. 5. 
$$P_{ino} = P_{eo} + H \cdot A_c \cdot (\alpha_c + \rho \cdot \rho_c) + \sum_j P_{rco_j} + P_{hco}$$

Eq. 6. 
$$P_{outo} = P_{co} + \sum_j P_{cro_j} + \sum_k P_{lco_k}$$

Where:

$P_e$  = cavity electrical heating

$P_{rc}$  = radiative inputs to cavity from FOV  $j$

$P_{lc}$  = loss by electrical lead conduction

$H$  = Total Solar Irradiance

$\alpha_c$  = effective cavity absorptance for TSI

$\rho_c$  = effective cavity reflectance for TSI

$P_{cr}$  = radiative outputs from cavity

$P_c$  = loss by thermal conduction to the heatsink

$A_c$  = Area of primary aperture

$\rho$  = effective cavity FOV reflectance for TSI

$P_{hc}$  = input to cavity heat capacity



# Active Cavity Radiometer measurements

The assumption of quasi-equilibrium requires that the sum of input and output power for the cavity in the reference and observations phases be nearly equal:

Eq. 7  $\sum P_{inr} \approx \sum P_{outr}$  (Reference phase)

Eq. 8  $\sum P_{ino} \approx \sum P_{outo}$  (Observation phase)

Solving for the electrical heating powers using Eq.'s 2 – 8 and put the equation in the form of eq. 1:

Eq. 9  $H = 1/[Ac(\alpha c + \rho \rho c)] \{ (P_{er} - P_{eo}) +$  (electrical power term)  
 $C \cdot (T_{dotr} - T_{doto})$  + (cavity heat capacity term)  
 $\sum_j (P_{crr_j} - P_{cro_j})$  - (radiation from cavity term)  
 $\sum_j (P_{rcr_j} - P_{rco_j})$  + (radiation to cavity term)  
 $\sum_j (P_{cr_j} - P_{co_j})$  + (thermal conductance term)  
 $\sum_j (P_{lcr_j} - P_{lco_j}) \}$  (electrical lead conductance term)

Where:  $C$  = cavity heat capacity,  $T_{dot}$  = thermal drift rate of cavity

# Active Cavity Radiometer measurements

- Discussion of the quasi-equilibrium equation
- Reduction of differential temperature terms to negligible values closely approximates equilibrium conditions. In practical measurements use of the following equilibrium equation is justified:

Eq. 10  $H = [Ac(\alpha c + \rho pc)]^{-1} \cdot \{(P_{er} - P_{eo}) + (P_{cr_1} - P_{co_1})\}$

Where:

$K = [Ac(\alpha c + \rho pc)]^{-1}$  Metrologically determined 'standard detector constant' of Eq. 1

$P_{er} - P_{eo}$  The difference in electrical substitution power supplied to maintain the same cavity thermal state in the reference and observation phases

$P_{cr_1} - P_{co_1}$  The difference in radiative transfer to the cavity from its view limiting aperture (field of view 1) in the shutter open and closed phases

# Active Cavity Radiometer measurements

- Cavity heating power term ( $P_{er} - P_{eo}$ ):

Eq. 11  $P_{er} = V_r \cdot I_r$

Eq. 12  $P_{eo} = V_o \cdot I_o$

Where:

$V_r, V_o, I_r, I_o$  are the cavity electrical heater voltages and currents in the shutter closed (reference) and shutter open (observations) phases of the measurement.

- Cavity heat capacity term:

Eq. 13  $C \cdot (T_{dot{r}} - T_{dot{o}})$

Where:

This term represents the net power transferred to or from the heat capacity ( $C$ ) of the cavity in the two phases of measurement.



# Active Cavity Radiometer measurements

- Radiation from the cavity to its surround  $\sum_j (P_{crr_j} - P_{cro_j})$  :

Eq. 14 
$$\sum_j P_{cr_j} = \sum_j \epsilon_{c_j} \cdot A_{c_j} \cdot \sigma \cdot T_{c_j}^4 \cdot F_{c_j}$$

- Radiation to cavity from surround term  $\sum_j (P_{rcr_j} - P_{rco_j})$  :

Eq. 15 
$$\sum_j P_{rc_j} = \sum_j \epsilon_j \cdot A_{c_j} \cdot \sigma \cdot T_j^4 \cdot F_{c_j}$$

Where:

$\epsilon_{c_j}$  = cavity infrared (IR) emittance to  $j^{\text{th}}$  field of view (FOV)

$\epsilon_j$  = infrared (IR) emittance of  $j^{\text{th}}$  FOV

$A_{c_j}$  = cavity area presented to  $j^{\text{th}}$  FOV

$\sigma$  = Stefan-Boltzmann constant

$T_{c_j}$  = temperature of cavity seen by  $j^{\text{th}}$  FOV

$T_j$  = temperature of  $j^{\text{th}}$  FOV

$F_{c_j}$  = radiative view factor between cavity and  $j^{\text{th}}$  FOV



# Active Cavity Radiometer measurements

- The  $4\pi$  steradian FOV of the cavity has been subdivided into five regions for the analysis of functional relationships between the cavity and its surround:

## FOV Description

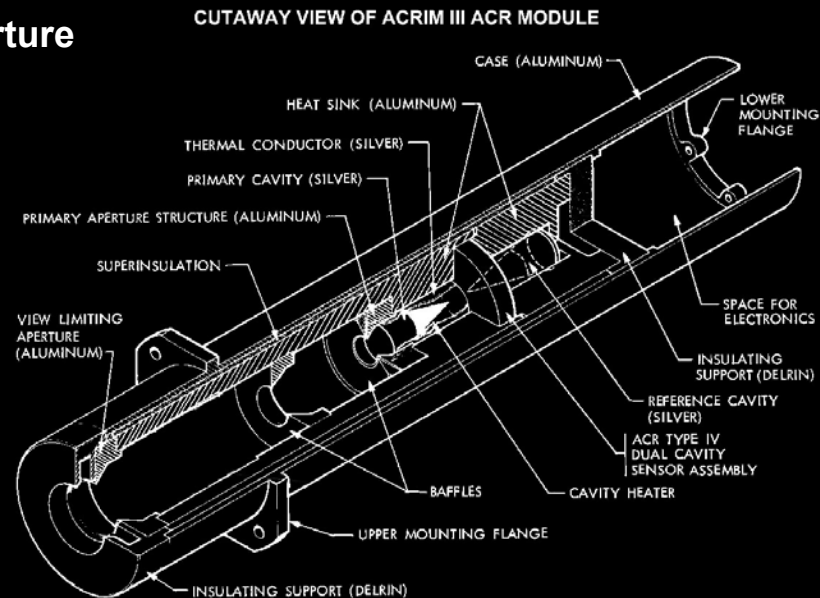
1 Cavity's view through its view limiting aperture (solar view)

2 Cavity's view of the heat sink extension-view limiting assembly

3 Cavity's view of underside of primary aperture

4 Cavity's view of thermal impedance

5 Cavity's view of heat sink



# Active Cavity Radiometer measurements

- Conductance to the heat sink from the cavity:

Eq. 16  $P_c = K_{tc} \cdot (T_c - T_s)$

Where:

$K_{tc}$  = thermal conductance from cavity to heatsink

$T_c$  = cavity temperature

$T_s$  = heatsink temperature

- Conductance to heatsink through leads :

Eq. 17  $\sum_k P_{lc_k} = \sum_k K_{lc_k} \cdot (T_c - T_s)$

Where:

$K_{lc_k}$  = thermal conductance of  $k^{\text{th}}$  electrical lead from cavity to heat sink



# Active Cavity Radiometer measurements

SYMBOL	UNITS	VALUE	UNCERTAINTY	DESCRIPTION
$\alpha_c$	-	0.9995	0.000002	cavity absorptance
$A_c$	cm <sup>2</sup>	0.500	0.0001	area of primary aperture
$\rho_c$	-	0.0005	0.0002	effective cavity reflectance for TSI
$\rho$	-	0.05	0.01	reflectance of cavity's FOV for TSI
$V_o$	volts	3.75	0.00015	cavity heater voltage - shutter open
$V_r$	volts	7.5	0.00015	cavity heater voltage - shutter closed
$I_o$	amps	0.008	0.00015	cavity heater current - shutter open
$I_r$	amps	0.013	0.00015	cavity heater current - shutter closed
$K_{th}$	mW/K	100	0.4	thermal impedance conductance
$K_{lc_k}$	mW/K	0.1	0.01	cavity electrical lead conductance
$\sigma$	mW-cm <sup>-2</sup> - K <sup>-4</sup>	$5.6697 \times 10^{-12}$	$7 \times 10^{-16}$	Stefan-Boltzmann constant
$C$	mW-sec-K <sup>-1</sup>	500	10	cavity heat capacity
$\epsilon_{1,2,3}$	-	0.98	0.02	cavity emittance to FOV's 1,2,3
$\epsilon_{4,5}$	-	0.05	0.05	cavity emittance to FOV's 4,5

# Active Cavity Radiometer measurements

SYMBOL	UNITS	VALUE	UNCERTAINTY	DESCRIPTION
$Ac_{1,2}$	cm <sup>2</sup>	0.5	0.00013	cavity areas seen by FOV's 1,2
$Ac_3$	cm <sup>2</sup>	1.3	0.13	cavity areas seen by FOV 3
$Ac_{4,5}$	cm <sup>2</sup>	5.0	0.2	cavity areas seen by FOV's 4,5
$\epsilon_1$	-	0.05	0.02	emittance of FOV 1
$\epsilon_{2,3}$	-	0.95	0.02	emittance of FOV's 2,3
$\epsilon_{4,5}$	-	0.05	0.02	emittance of FOV's 4,5
$T_c$	K	300.5	2	cavity temperature
$T_{1,2,3,5}$	K	301	2	temperatures of FOV's 1,2,3,5
$T_4$	K	300.5	2	temperatures of FOV 4
$\delta T_c$	K	0.01	-	cavity temperature drift per cycle
$\delta T_1$	K	10	-	FOV 1 temperature drift per cycle
$\delta T_{2,3,4,5}$	K	.1	-	FOV's 2,3,4,5 temp. drift per cycle
$Fc_1$	-	$8 \times 10^{-2}$	$5 \times 10^{-4}$	cavity view factor to FOV 1
$Fc_2$	-	0.923	$6 \times 10^{-5}$	cavity view factor to FOV 2
$Fc_3$	-	0.704	$5 \times 10^{-2}$	cavity view factor to FOV 3
$Fc_4$	-	0.8	0.08	cavity view factor to FOV 4
$Fc_5$	-	0.2	0.02	cavity view factor to FOV 5

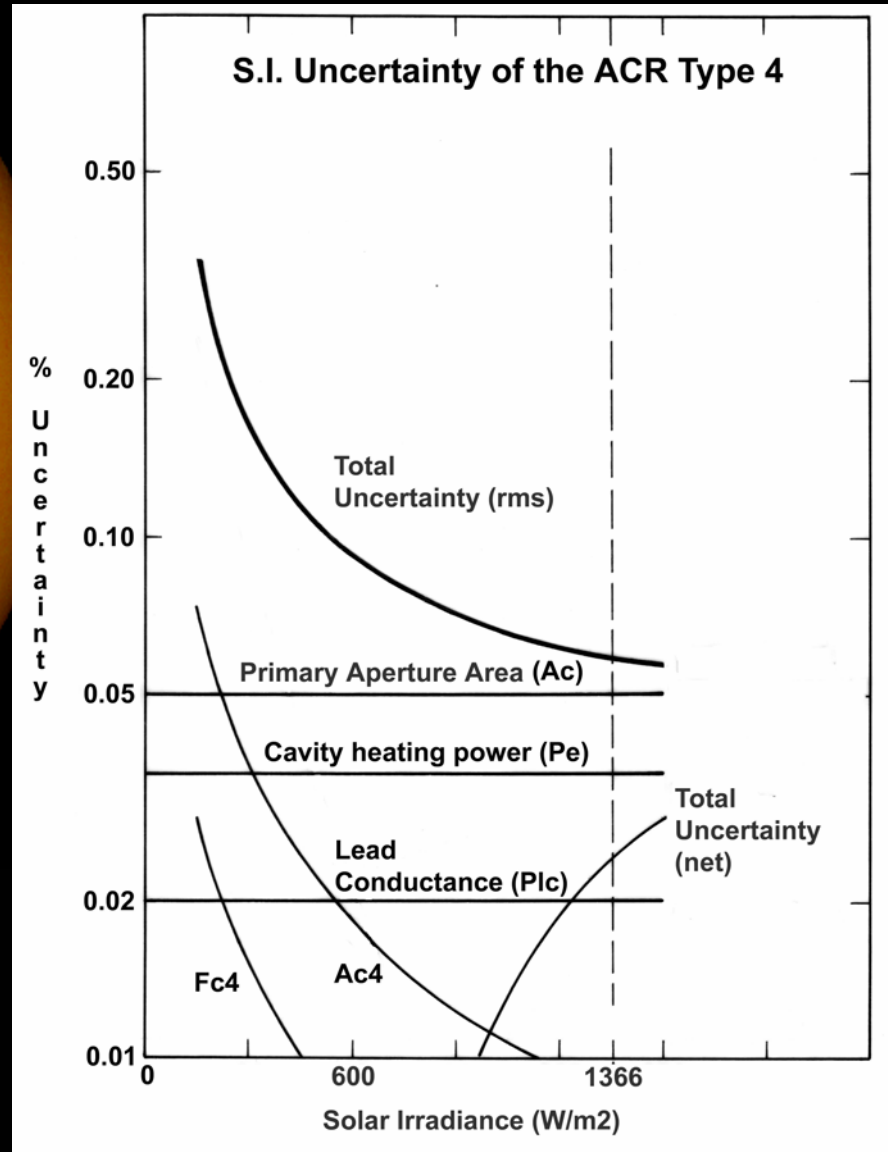
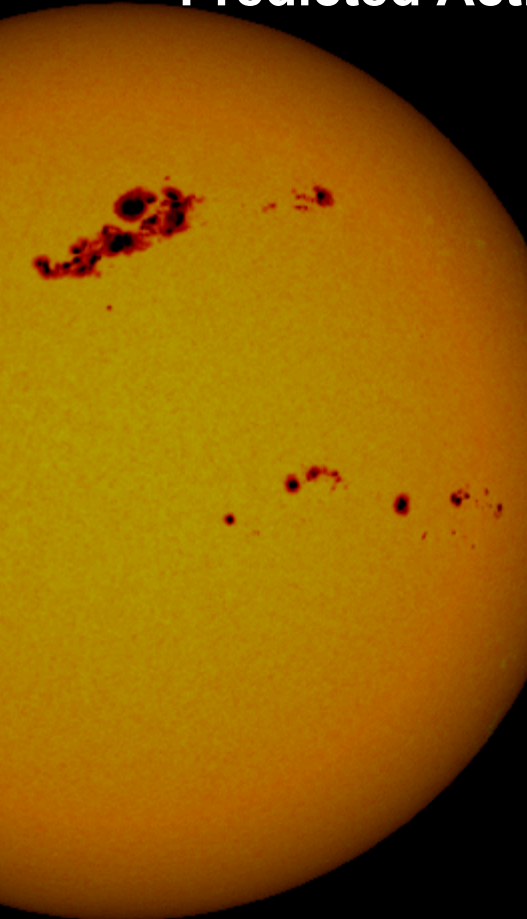
# Active Cavity Radiometer Measurements

- ACRIM design based on passive realization of small measurement phase temperature differences
- To the extent this is achieved, the quasi-equilibrium equation ( Eq. 9) can be simplified using Taylor expansions about reference phase temperatures:

Eq. 18

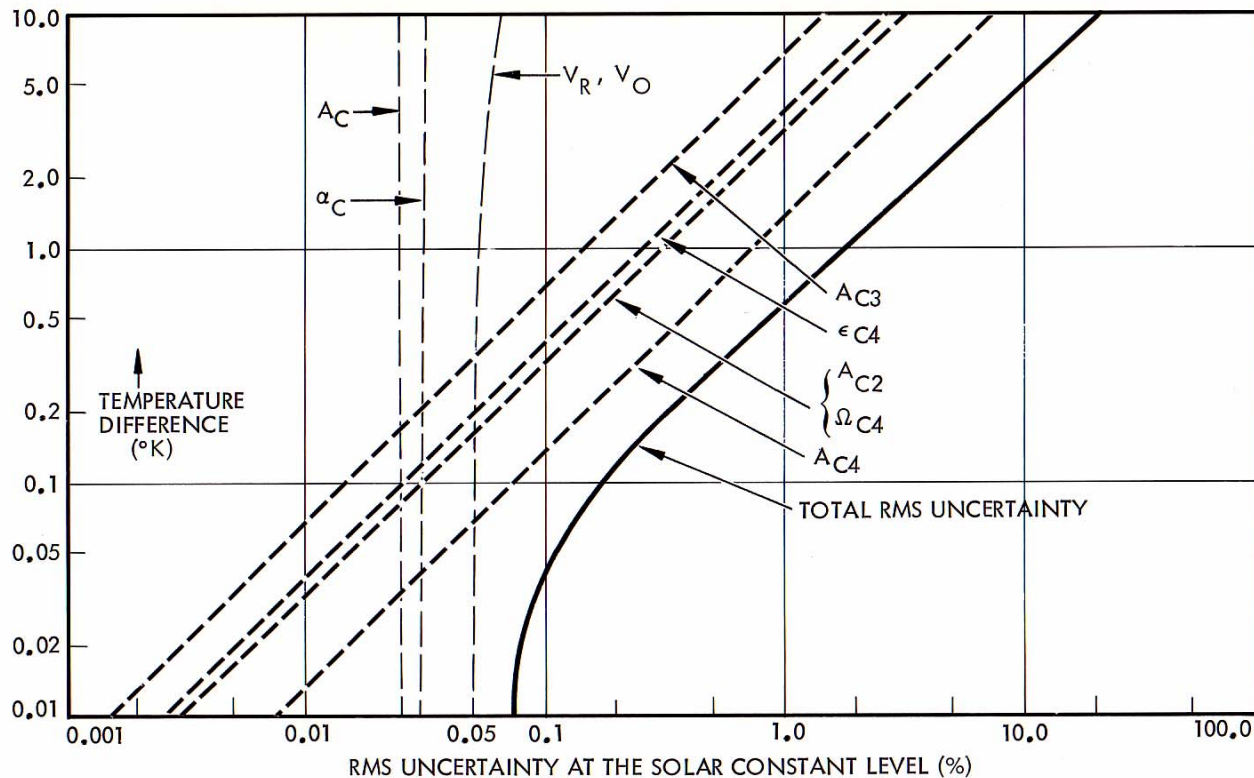
$H = 1/[Ac(\alpha c + \rho pc)] \{(Per - Peo) +$		(electrical power)
$C \cdot (Tdotr - Tdoto)$	$\rightarrow - C \cdot \delta Tdotr$	(cavity heat capacity)
$\sum_j (Pcrr_j - Pcroj)$	$\rightarrow - 4 \cdot \sigma \cdot \sum_j Ac_j \cdot Fc_j \cdot \epsilon c_j \cdot Tcrr_j^3 \cdot \delta Tcrr_j$	(radiation from cavity)
$\sum_j (Pr cr_j - Prco_j)$	$\rightarrow - 4 \cdot \sigma \cdot \sum_j Ac_j \cdot Fc_j \cdot \epsilon j \cdot Tr cr_j^3 \cdot \delta Tr cr_j$	(radiation to cavity)
$(Pcr - Pco)$	$\rightarrow - Ktc \cdot (\delta Tcr - \delta T5r)$	(thermal conductance)
$\sum_k (Plcr_k - Plco_k)\}$	$\rightarrow - \sum_k Klc_k \cdot (\delta Tcr - \delta T5r)$	(lead conductance)

# Predicted Active Cavity Radiometer Uncertainties in S.I. Units



# Predicted Active Cavity Radiometer Uncertainties caused by thermal drifting between measurement phases

RMS UNCERTAINTY OF ACR IV AS A FUNCTION OF INSTRUMENT TEMPERATURE DIFFERENCE



KEY:  $A_C \equiv$  PRIMARY APERTURE AREA

$\alpha_C \equiv$  CAVITY ABSORPTANCE

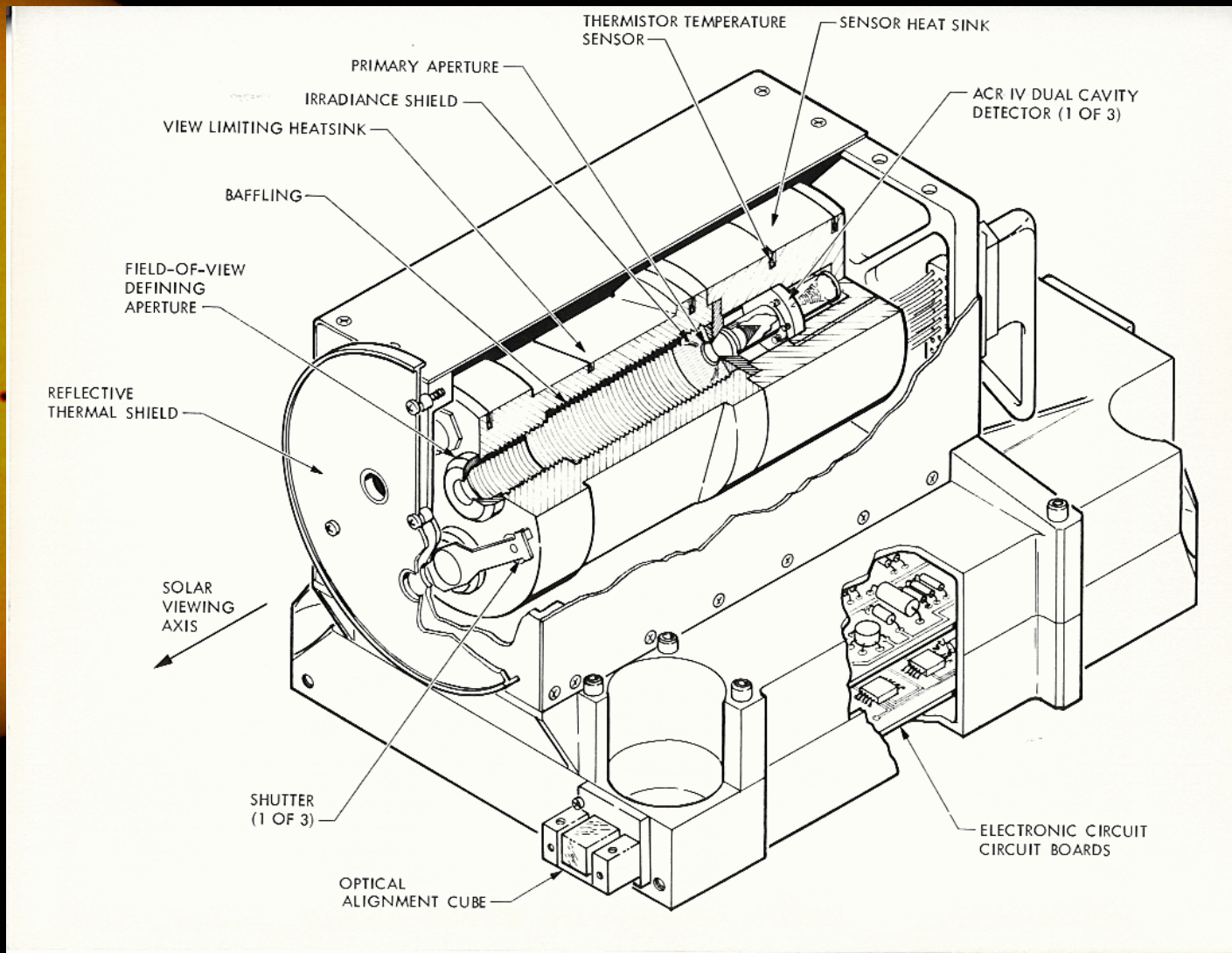
$V_R, V_O \equiv$  CAVITY HEATER POWER VOLTAGES  
(REFERENCE AND OBSERVATION PHASES)

$A_{2,3,4} \equiv$  CAVITY AREA SEEN BY FIELDS-OF-VIEW 2,3,4

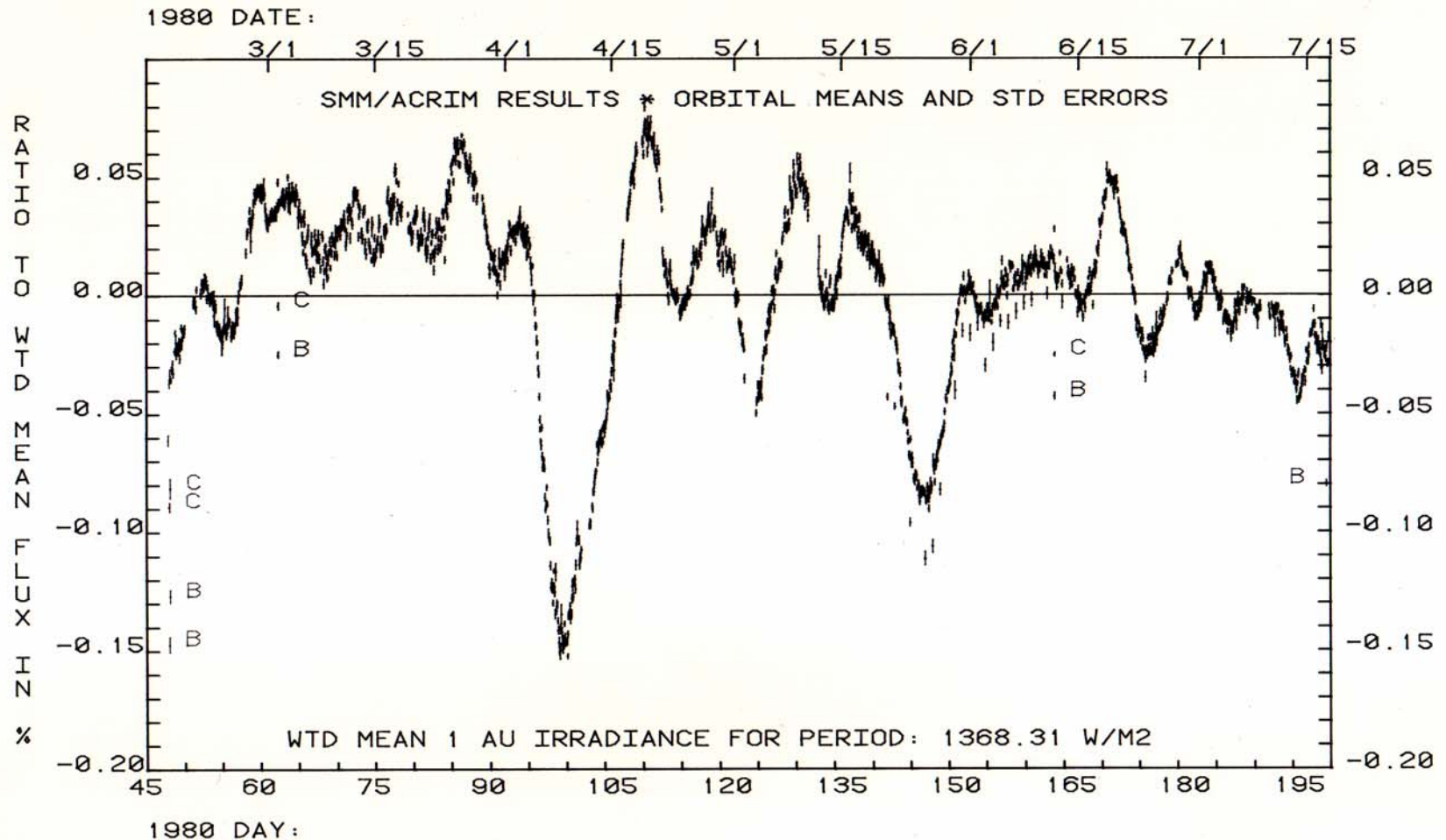
$\epsilon_{C4} \equiv$  CAVITY EMITTANCE TO FIELD-OF-VIEW 4

$\Omega_{C4} \equiv$  CAVITY FIELD-OF-VIEW 4

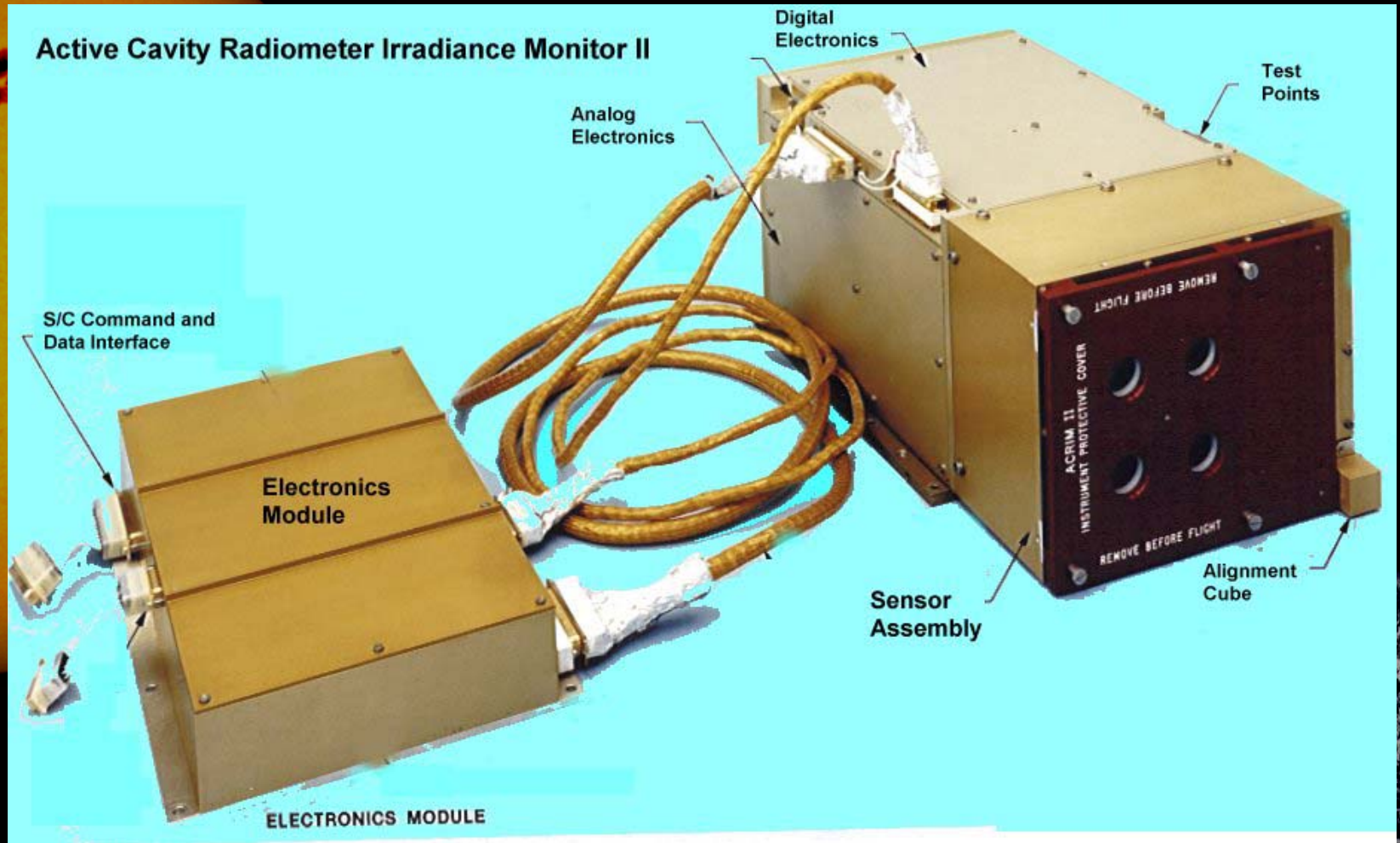
# SMM/ACRIM1 Instrument



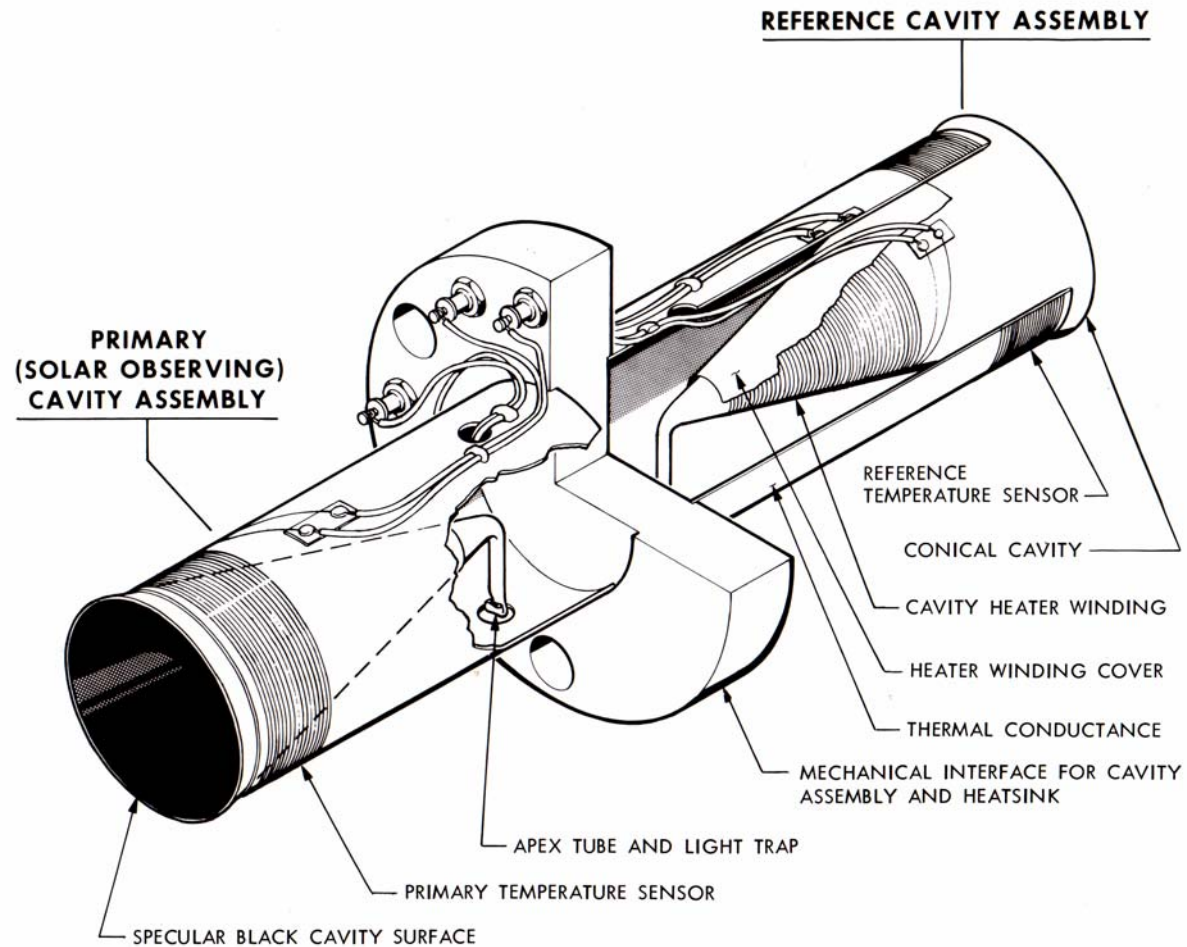
# SMM/ACRIM1 Early Mission Comparisons



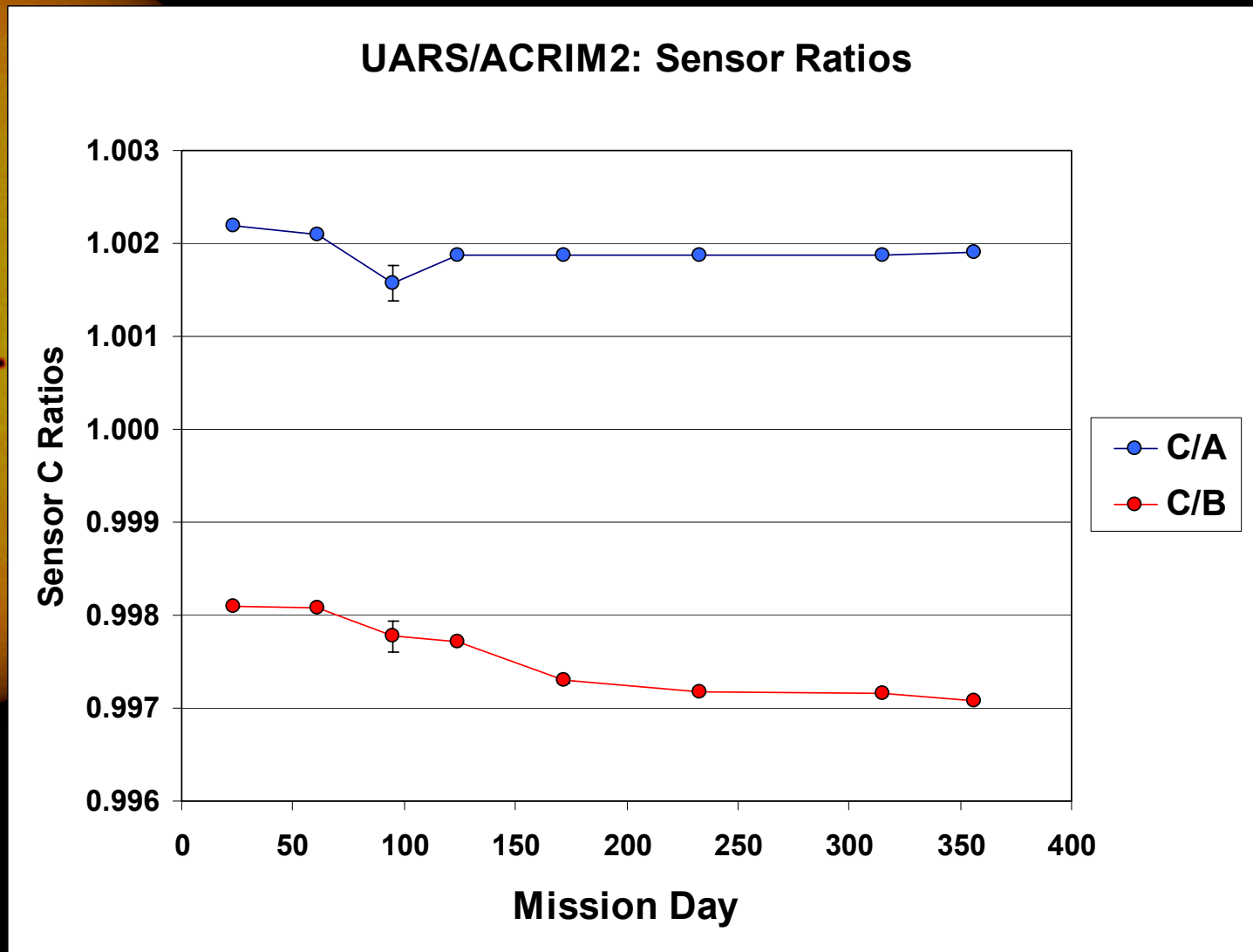
# UARS/ACRIM2 Instrument



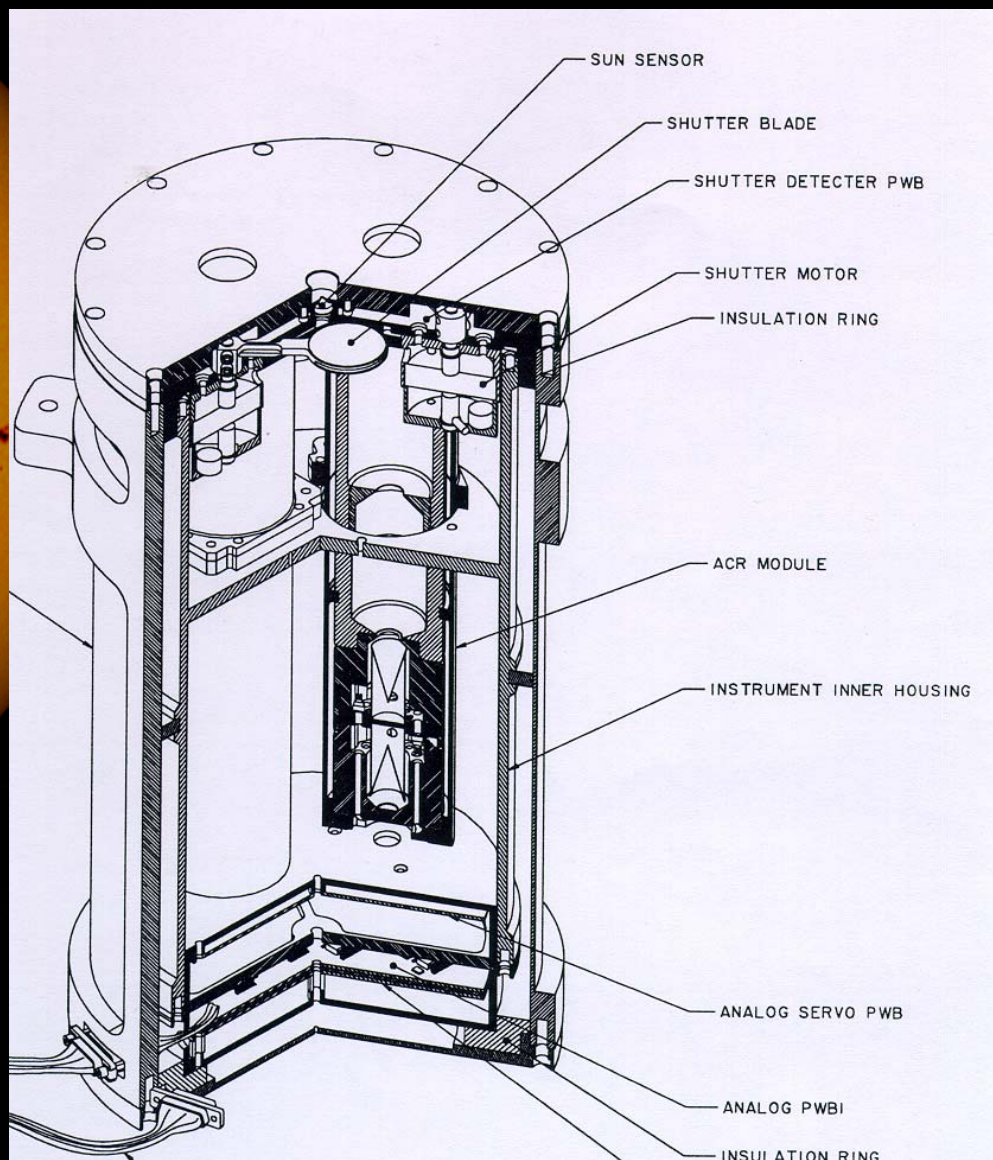
# UARS/ACRIM2 ACR Type V Cavity



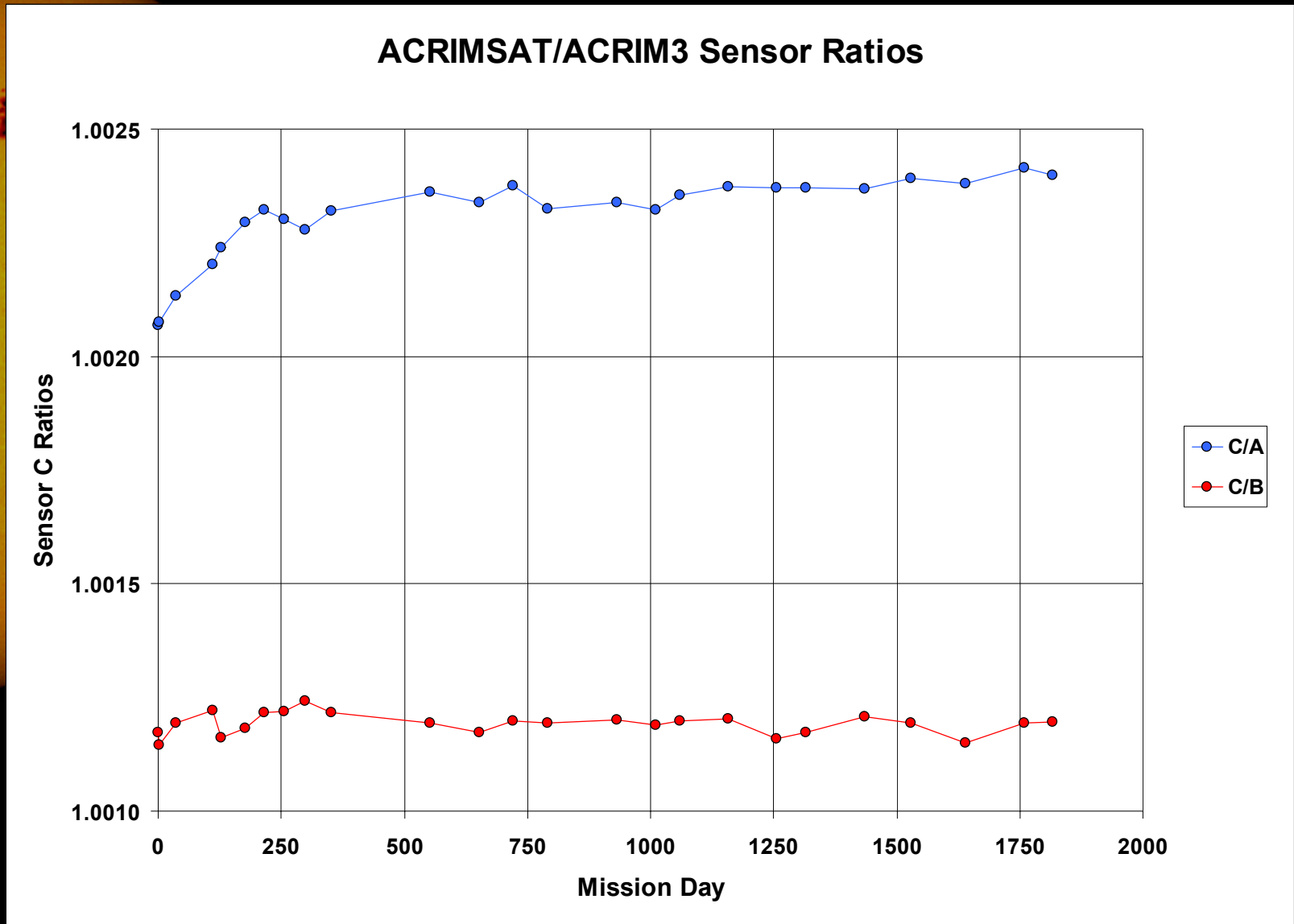
# UARS/ACRIM2 Sensor Comparisons – 1<sup>st</sup> Year



# ACRIM3



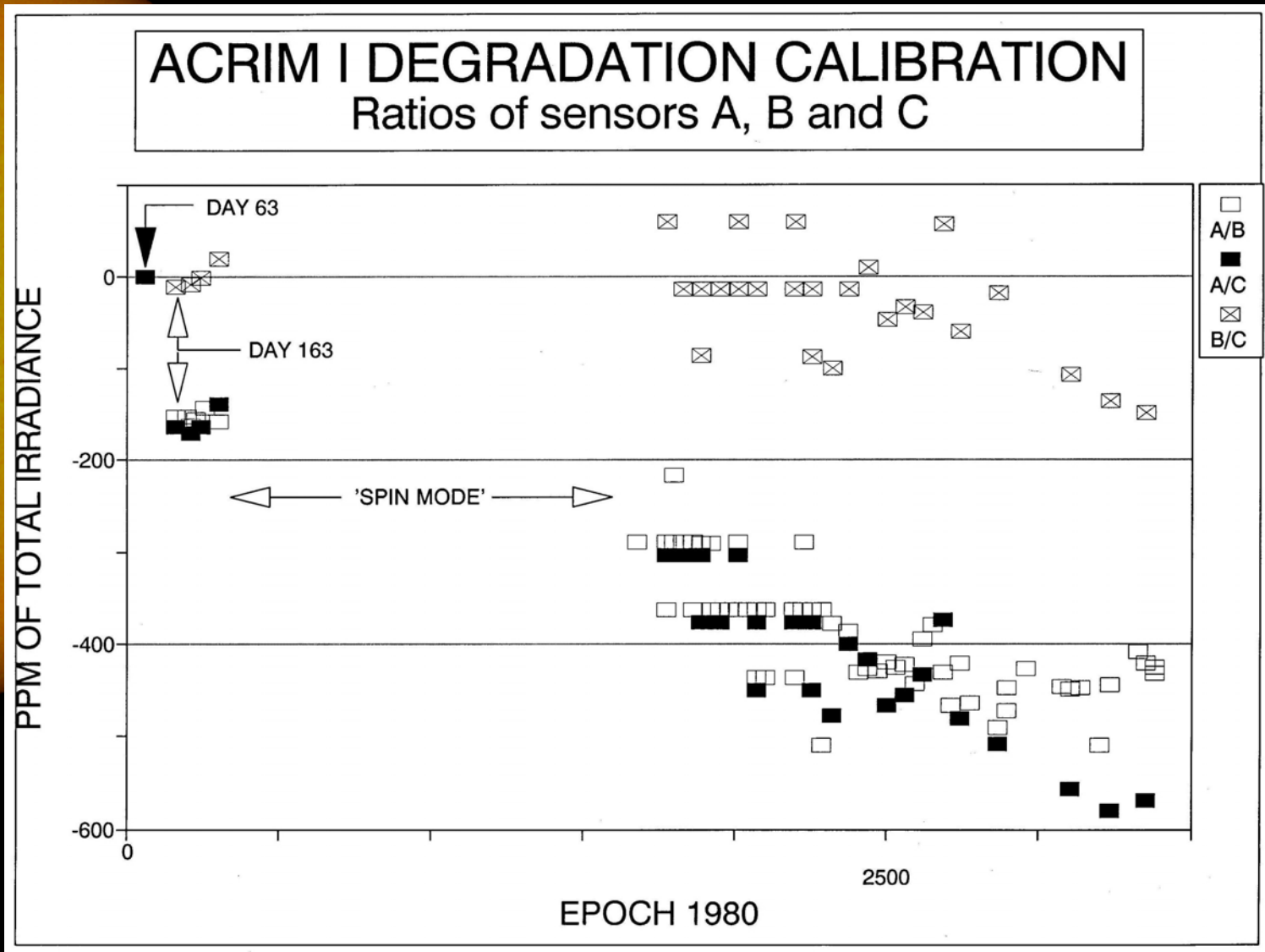
# ACRIM3 Comparisons and Degradation



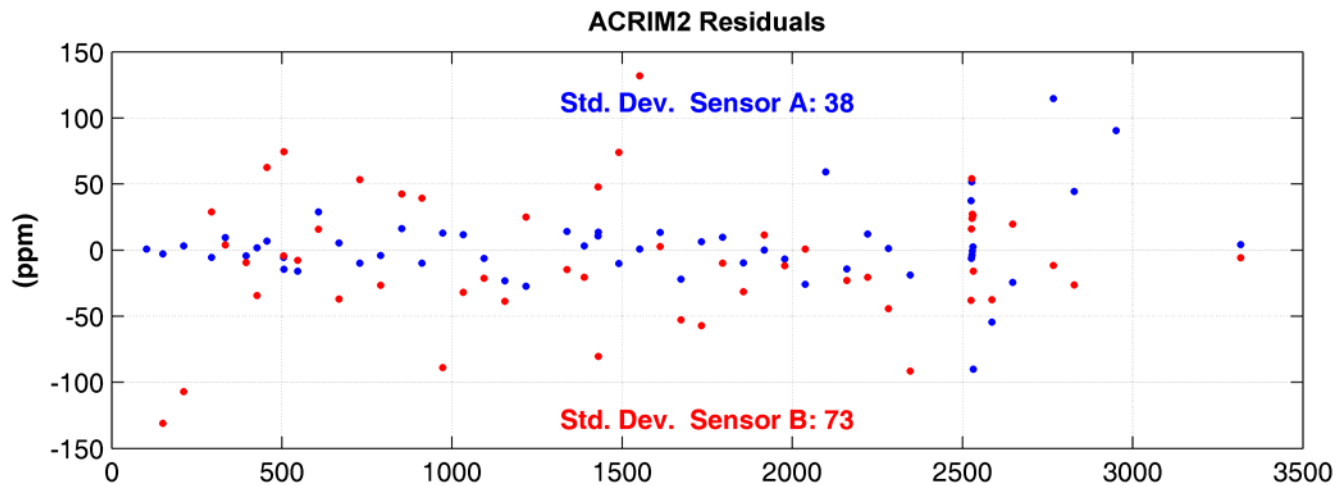
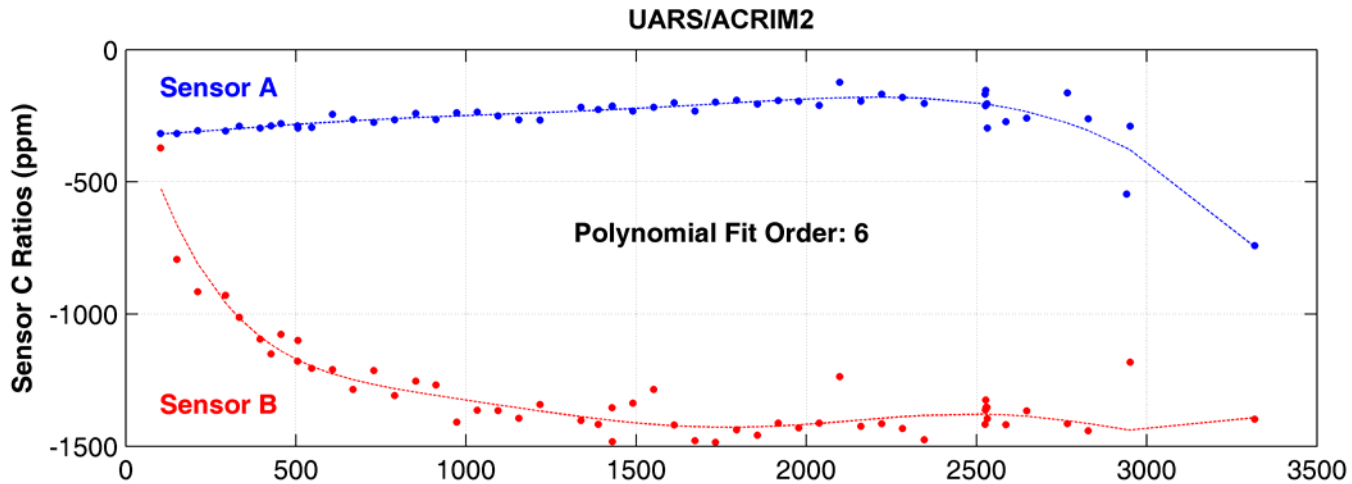
# ACRIM 'as-launched' Sensor Comparisons

Sensor Experiment	C/A ratio	C/B ratio	A/B ratio	Range %
SMM/ACRIM1	0.999480	1.000501	1.001021	0.1021
UARS/ACRIM2	1.002187	0.998088	0.995910	0.4090
ACRIMSAT/ACRIM3	1.002068	1.001174	0.999108	0.2068

# ACRIM1 Comparisons & Degradation Calibrations

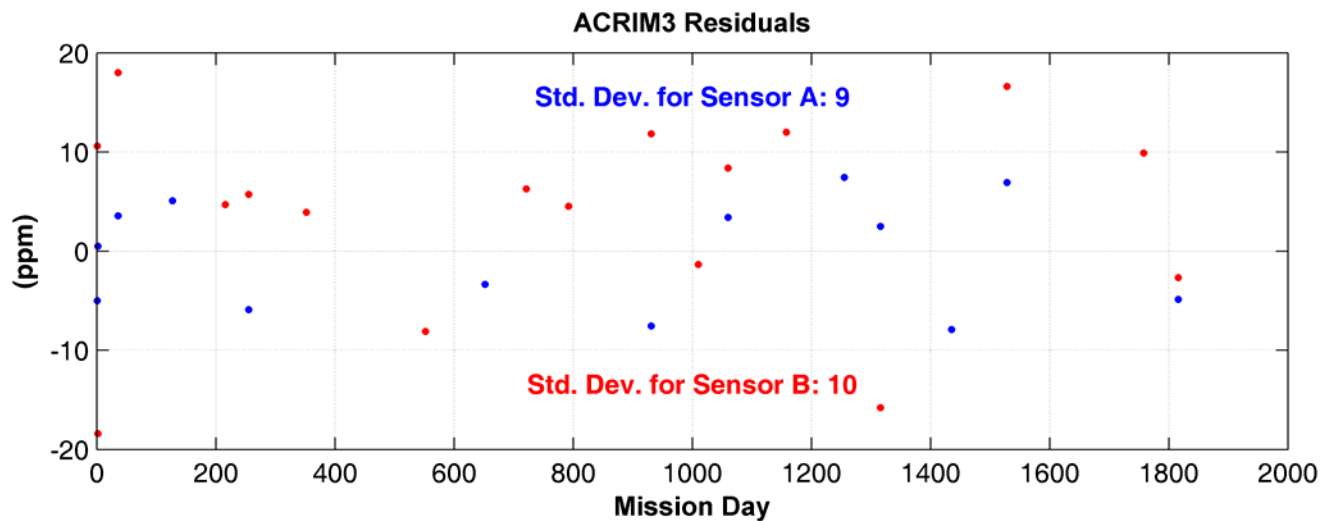
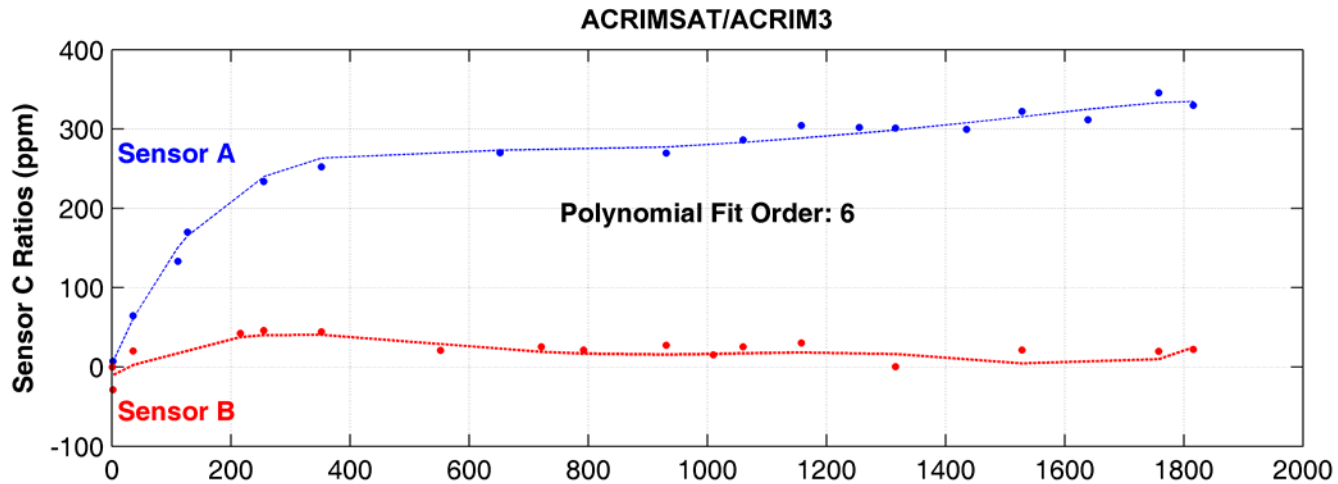


# ACRIM2 Comparisons and Degradation



RC Willson - Earth\_Obs\_fig7\_acrim2 07/14/2005

# ACRIM3 Comparisons and Degradation



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